

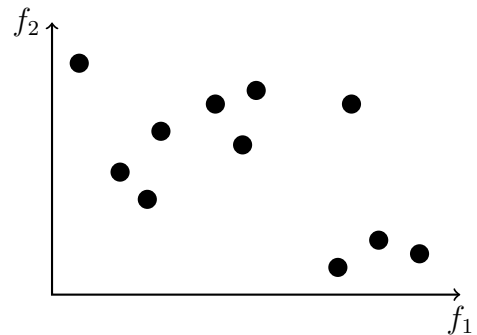
6. Exercise Sheet

Exercise 1 Methods for solving MOPs

- a) Describe the basic structure of one a priori and one a posteriori method for solving MOPs. Name their advantages and disadvantages.

Exercise 2 Ranking method

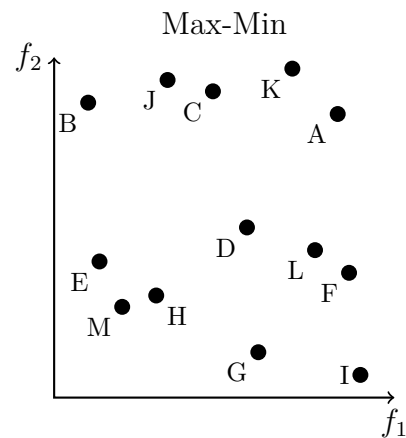
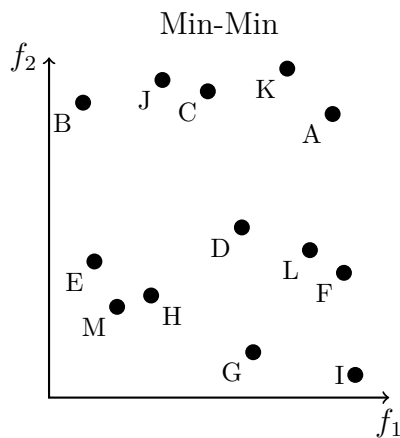
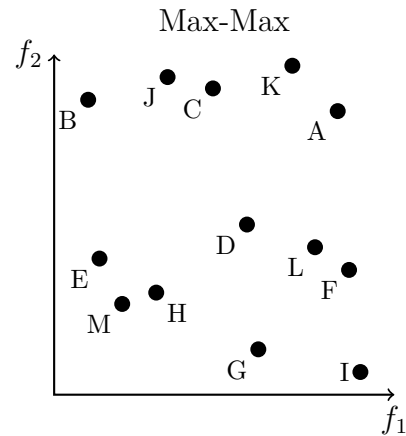
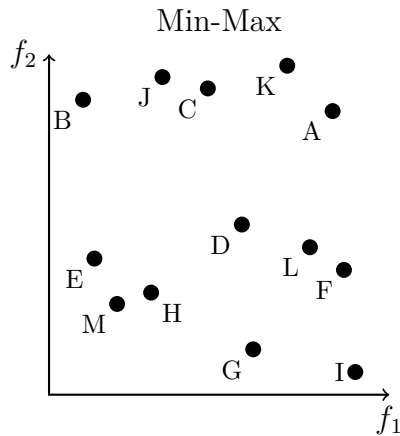
- a) Rank all the particles in terms of the number of superior individuals by which they are dominated when both features need to be minimized.
- b) This measure in the first subtask does only optimize the convergence of the pareto-front. Name and describe an alternative method, which takes the divergence of solutions into account.



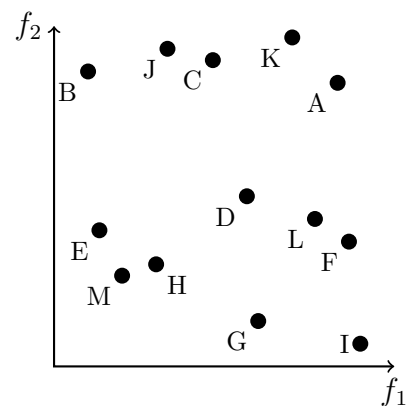
See the next two pages for the remaining tasks!

Exercise 3 Pareto-Fronts and NSGA-II

- a) Determine the Pareto-Front for all combinations of minimization and maximization of features f_1 and f_2 . You can just mark the individuals of the Pareto-Front in each of the following plots.

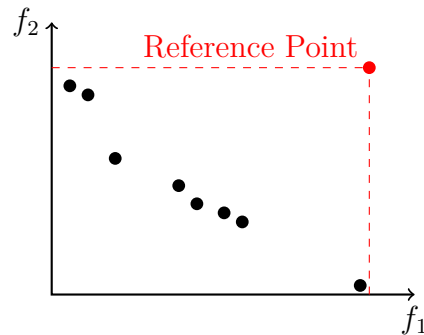


- b) In the following set of solutions shown in the objective space (assuming minimization of both objectives), identify the different non-dominated fronts of solutions by using the concept of the NSGA-II algorithm.
- c) Which solutions will be selected for the next population using crowding distance if we have a population size of 8?



Exercise 4 Marginal Hypervolume

- a) Which one of the following solutions has the largest marginal HV?
- b) Which one of the following solutions has the smallest marginal HV?



x	y
0.2	2.3
0.4	2.2
0.7	1.5
1.4	1.2
1.6	1.0
1.9	0.9
2.1	0.8
3.4	0.1
3.5	2.5

Exercise 5 Hypervolume

Suppose we are comparing two sets of non-dominated points A and B with each other using their hypervolume.

- a) For which of the following scenarios can the following inequality be true: $HV(A) < HV(B)$? Remember that the hypervolume needs to be computed on all points ($A = \bullet$, $B = \blacksquare$).
- b) How does the position of the reference point influence the comparison of A and B?

